

Analysis of influencing factors of PM_{2.5} based on regression equation

Jingrong Sun¹

¹*School of Information and Science Technology, Jinan University,
Guangzhou, 510000, China, E-mail:1196972348@qq.com*

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Abstract. According to the AQI data and the meteorological data of Xi'an in the last years, the relationships and the influence principles between PM_{2.5} and other five monitoring indicators of AQI, weather factors and heating time were analyzed, respectively, by the regression analysis and the ridge regression analysis. The main results include: (1) There were positive correlations between PM_{2.5} and SO₂, NO₂ and CO, which shows that SO₂, NO₂ and CO may be the major gaseous components of forming PM_{2.5}. Therefore, the concentration of PM_{2.5} can be reduced by considering how to efficiently decrease the concentrations of SO₂, NO₂, and CO. (2) The relationships between PM_{2.5} and temperature, sea level press, visibility, wind speed and accumulated precipitation are significantly negatively correlated based on the multiple regression. (3) The concentration of PM_{2.5} during the heating period was 1.868 times higher than that during non-heating period. Finally, the ridge regression between PM_{2.5} and all the factors mentioned above shows that SO₂, NO₂, PM₁₀, CO and heating time were more significant than others.

Keywords: PM_{2.5}, Air Quality Index, meteorological factors, heating period, multiple regression, ridge regression.

1. Introduction

SQI(Air Quality Index) is a dimensionless index quantitatively describing air quality, which has six basic indexes: SO₂、NO₂、PM₁₀、CO、O₃ and PM_{2.5}^[1-3].The PM_{2.5} is the emission of particles less than 2.5μm, which is one of the main reasons for producing fog and haze weather^[4-10]. All kind of toxic and hazardous substances adsorbed by PM_{2.5}, such as virus, can be inhaled into the respiratory system directly into the blood, which will the incidence of lung cancer, heart disease and chronic bronchitis^[11-15]. Therefore, it is not only very necessary but also urgent to monitor mass concentration of PM_{2.5} and analyze its pollution characteristics and influencing factors, which plays an important part to harness and predict PM_{2.5} effectively^[16].

But now when most of the papers come to discuss the influencing factors they involved nothing but AQI, meteorological factors and heating time. For example, Liu et al^[17] draw the conclusions that the relationship between PM_{2.5} and SO₂, NO₂, PM₁₀ and CO are positive correlations while the relationship between PM_{2.5} and O₃ are negative positive. Wang et al^[18] draw the conclusion that the relationship between PM_{2.5} and SO₂, NO₂ and OX(NO₂+O₃) are positive correlations; Zhang et al^[19] draw the conclusion that the relationship between PM_{2.5} and temperature is positive correlation, while the relationships between PM_{2.5} and wind speed ,relative humidity and air pressure are negative correlation. Chen et al^[20-22] draw the conclusion that the relationships between PM_{2.5} and temperature and wind speed are negative correlation while the relationships between PM_{2.5} and humidity and air pressure are positive correlation. Chen et al^[23] draw the conclusion that the relationships between PM_{2.5} and temperature, humidity, wind speed, wind direction and precipitation are significantly. When it goes to discuss PM_{2.5}, there is little paper take AQI, meteorological factors and heating time into consider at the same time, and there is also little paper considering heating time when they analyze PM_{2.5} by establishing regression equation^[24-25].

Basing to the studies having done, this paper selects the object, Xi'an, to analyze for its special location, Guangzhong Plain, surrounded by mountains in the south and Loess Plateau in the north, which limit the dispersion of air pollutants, and the observation of satellite indicates that the Xi'an is one of the most polluted cities^[26-28]. This paper considers every factor fully when we study the relationship and regression between PM_{2.5} and other factors, including other five basic indexes of AQI, seven meteorological factors and heating time.

2. Materials and methods

2.1.Data and sources

Data of AQI is downloaded in <http://www.xianemc.gov.cn/> including six basic indicators data. Data of meteorology is downloaded in <https://www.wunderground.com/> including temperature, the dew point, humidity, sea level pressure, visibility, wind speed and precipitation. Data of longitude and altitude of thirteen areas in Xi'an is downloaded in <http://haiba.qhdi.com/>.

2.2.research method

When the relationship between PM_{2.5} and heating time is analyzed, we consider 2015-3-1 to 2015-3-15 and 2015-11-15 to 2016-2-29 as heating period, and 2015-3-16 to 2015-11-14 to as non-heating period according to Xi'an's polices. In this paper, we discuss the relationship between PM_{2.5} and its influencing factors, mainly by using the method of multiple regression equation. However, in order to avoid multicollinearity, ridge regression equation between PM_{2.5} and other indexes of AQI, meteorological factors and heating time is built.

3. Results and discussion

Following, we are going to analyze the influencing factors of PM_{2.5} concentration. The relationships between PM_{2.5} and AQI, meteorological factors and heating time are analyzed in section 2.1, 2.2 and 2.3, respectively.

3.1. Ridge regression analysis of PM_{2.5} and other monitoring indexes in AQI

The multiple regression equation is established with the variable of PM_{2.5} as the dependent variable, and SO₂(x₁), NO₂(x₂), PM₁₀(x₃), CO(x₄) and O₃(x₅) as independent variables. As is shown in Fig 1, the relationship is significantly correlated with each monitoring indicator of AQI, therefore, we adopt the ridge regression to avoid multicollinearity. After analyzing, the ridge regression equation of PM_{2.5} to x₁, x₂, x₃, x₄ and x₅ is

$$\hat{y}_{PM_{2.5}} = -16.386 + 0.622x_1 + 0.375x_2 + 0.404x_3 + 0.619x_4 - 0.011x_5. \tag{1}$$

The standard ridge regression equation is

$$\hat{y}_{PM_{2.5}} = 0.150x_1 + 0.135x_2 + 0.315x_3 + 0.212x_4 - 0.006x_5 \tag{2}$$

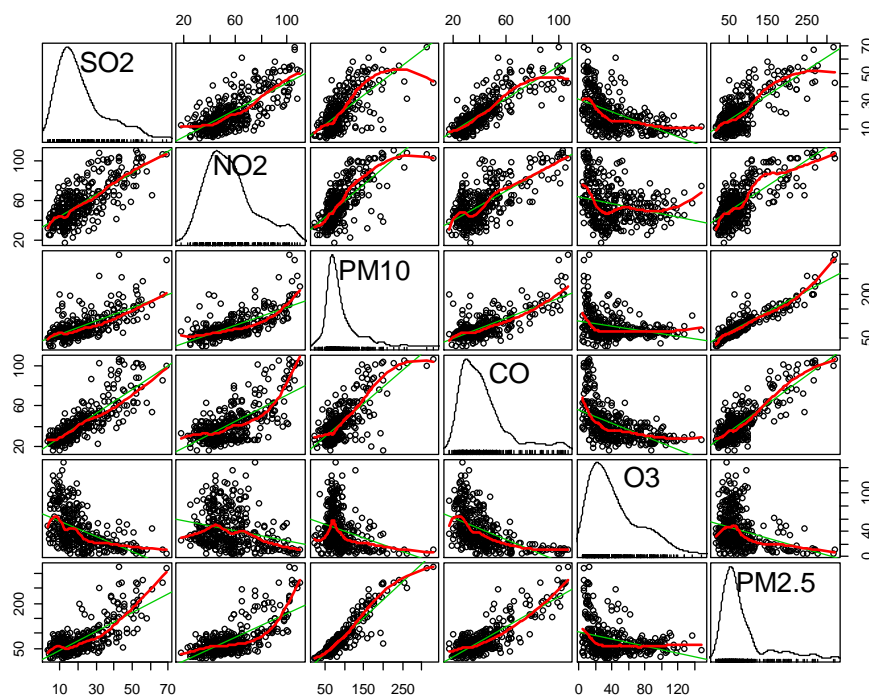


Fig.1 Matrix scatter diagram of AQI monitoring indicators

The standard ridge regression equation indicates that there are high positive correlation between PM_{2.5} and SO₂(x₁), NO₂(x₂), PM₁₀(x₃) and CO(x₄), so we can speculate that PM_{2.5} may be formed by those polluted gases. The relationship between PM_{2.5} and O₃(x₅) is negative correlation. The standard ridge regression equation shows that, when other factors are fixed, PM_{2.5} concentration adds 0.15 units when SO₂ concentration rose for every one unit and so on.

The influencing principles between PM_{2.5} and other polluted gases are as followed: the incomplete combustion of fossil fuels produce not only CO but also PM_{2.5}; NO₂ can generating nitrogen oxides and ammonia, and SO₂, nitrogen oxides and ammonia can converted into PM_{2.5} under certain circumstances, thus, PM_{2.5} should have a positive correlation with CO, SO₂ and NO₂; but O₃ can oxide CO, SO₂ and NO₂, further to resist the rising of PM_{2.5} concentration, thus PM_{2.5} should have a negative correlation with O₃.

3.2. Multiple regression analysis of PM_{2.5} and meteorological factors

The multiple regression equation is established with the variable of PM_{2.5} as the dependent variable, and temperature(x₆), the dew point(x₇), humidity(x₈), sea level pressure(x₉), visibility(x₁₀), wind speed(x₁₁) and precipitation(x₁₂) as independent variables. Regression diagnosis of regression equation found residual does not satisfy the Gauss Markov assumptions, so the model should be built after having a logarithmic transformation to explained variable. After eliminating not significant explanatory and collinearity, multiple regression equations is as follows:

$$\log(\hat{y}_{PM_{2.5}}) = 24.456 - 0.017x_6 - 0.019x_9 - 0.129x_{10} - 0.011x_{11} - 0.019x_{12} \tag{3}$$

The p value of t test of regression equation is 4.68e-65, and both the constant and linear terms of regression equation are significant under the significant level of 0.05. The regression equation indicates that the relationships between PM_{2.5} and temperature, sea level pressure, visibility, wind speed and the cumulative precipitation are significantly negatively correlated. The equation shows that when other factors are fixed, PM_{2.5} concentration adds 0.15 units when temperature rose for every one unit and so on.

The regression diagnostic plots showed that residual values were satisfied with the equal variance, independent variance and normal distribution, therefore, the model of regression equation pass the test.

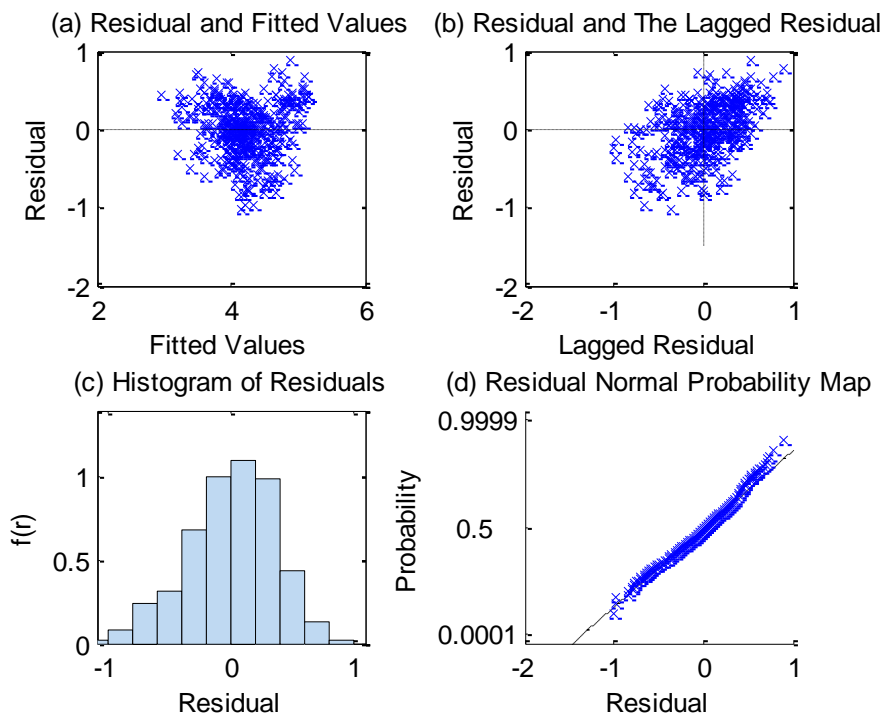


Fig.2 Regression diagnostic residuals

The influencing principles between PM_{2.5} and meteorological factors are as followed: the relationship between PM_{2.5} concentration and temperature is negative correlation. The reason why their relationship is negative correlation is that the temperature increases, the solar radiation and the atmospheric turbulence increase, making the air flow and the mixing layer become larger, which can promote the diffusion and

dilution of $PM_{2.5}$ [20]. The relationship between $PM_{2.5}$ and sea level pressure is negative correlation. The reason why their relationship is negative correlation is that when the pressure decrease, which will make the wind speed decrease thus to resist the diffusion of $PM_{2.5}$, the $PM_{2.5}$ concentration will increase [19]. The reason why the relationship between $PM_{2.5}$ and visibility is negative correlation is that the high $PM_{2.5}$ concentration can not only diffuse but also absorb light to decrease the visibility [23,28]. The reason why the relationship between $PM_{2.5}$ and accumulated precipitation is negative correlation is that precipitation can scour the $PM_{2.5}$ in the air. It is easy to understand that why the relationship between $PM_{2.5}$ and wind speed is negative correlation is that the higher wind speed the more beneficial to the diffusion of $PM_{2.5}$. In addition, there is little papers analyzing the $PM_{2.5}$ concentration by combining with the cumulative wind speed, wind direction and altitude of thirteen monitoring stations in Xi'an at the same time. Therefore, the further analysis draw the conclusion showing in Fig.3 that the northeast is the main wind direction and the altitude is gradually increasing from the northwest to the southeast in Xi'an. The $PM_{2.5}$ concentration in the districts of Yanliang and Lintong may be lower, because those districts are located in the northeast direction, direction of air inlet. The $PM_{2.5}$ concentration in the districts of Guangyuntan and Fangzhicheng may be higher, for not only they are located in the direction of air outlet of Lintong and lower altitude than Lintong, but also the altitude in the direction of air outlet of Guangyuntan and Fangzhicheng is higher than Guangyuntan and Fangzhicheng's. Contrary to Guangyuntan and Fangzhicheng, Xingqinxiaoqu's $PM_{2.5}$ concentration may be lower, because not only Xingqinxiaoqu is not be polluted by the direction of air inlet, but also the altitude in the areas of the direction of air outlet is lower than Xingqinxiaoqu.

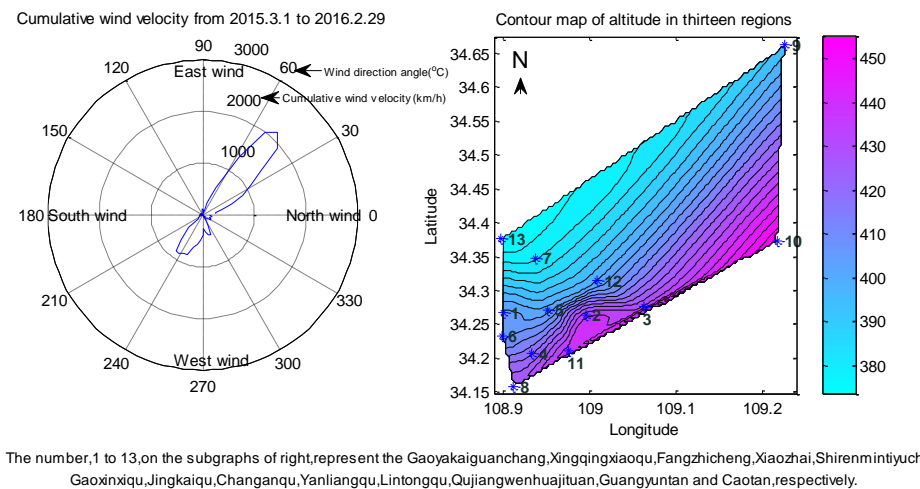


Fig.3 The comparison between wind and $\rho(PM_{2.5})$ contour map

3.3. Analysis on the relationship between $PM_{2.5}$ and heating period

After a series of calculations, the mean value of $PM_{2.5}$ concentration is 116.059 during heating period, while 62.135 during non-heating period. In other word, it means that mean value of $PM_{2.5}$ concentration during heating period is 1.868 times as much as the mean value during non-heating period, which indicates that the combustion of coal during heating period has a great impact on the rise of $PM_{2.5}$ concentration. Therefore, on the one hand, it is necessary for government to take emergency measure to improve the technology to produce coal of high quality; on the other hand, we should advocate the use of low emission energy, such as natural gas.

3.3. Comprehensive analysis of relationship between $PM_{2.5}$ and other indexes of AQI, meteorological factors and heating time

The multiple regression equation is established with the variable of $PM_{2.5}$ as the dependent variable, and $SO_2(x_1)$, $NO_2(x_2)$, $PM_{10}(x_3)$, $CO(x_4)$, $O_3(x_5)$, temperature(x_6), the dew point(x_7), humidity(x_8), sea level pressure(x_9), visibility(x_{10}), wind speed(x_{11}), precipitation(x_{12}) and heating time(x_{12}) as independent variables. In the equation, heating time is a dummy variable, in which the value 1 represents heating period, while value 0 represents not-heating period. Taking into account the explanatory variables too many, we adopt the ridge regression to avoid multicollinearity. After analyzing, the ridge regression equation is

$$\hat{y}_{PM_{2.5}} = -13.407 + 0.733x_1 + 0.221x_2 + 0.565x_3 + 0.641x_4 + 0.543x_7 - 3.354x_{10} + 3.235x_{13} \quad (4)$$

The standard ridge regression equation is

$$\hat{y}_{PM_{2.5}} = 0.176x_1 + 0.080x_2 + 0.440x_3 + 0.220x_4 + 0.105x_7 - 0.138x_{10} + 0.028x_{13} \quad (5)$$

The goodness of fit of multivariate linear regression giving above is 0.952. The standard ridge regression equation indicates that SO₂(x₁), NO₂(x₂), PM₁₀(x₃), CO(x₄), the dew point(x₇), visibility(x₁₀) and heating time(x₁₂), compared to other factors, have a significant impact on PM_{2.5}. The standard ridge regression equation shows that, when other factors are fixed, PM_{2.5} concentration rise 0.176 units when SO₂ concentration rose for every one unit; and PM_{2.5} concentration during heating time is 0.028 units higher than PM_{2.5} concentration during non-heating time and so on.

4. Conclusion

a) In the analysis of PM_{2.5} and other five monitoring indicators of AQI, there are high positive correlation between PM_{2.5} and SO₂(x₁), NO₂(x₂), PM₁₀(x₃) and CO(x₄), so we can speculate that PM_{2.5} may be formed by those polluted gases. Therefore, we can decrease PM_{2.5} concentration by thinking about how to effectively reduce those polluted gases.

b) In the analysis of PM_{2.5} and meteorological factors, not only the multiple regression of PM_{2.5} and meteorological factors is giving, but also the influencing principles between PM_{2.5} and meteorological factors are giving, which has an important guiding significance to predict the trend of PM_{2.5}.

c) In the analysis of PM_{2.5} and heating time, mean value of PM_{2.5} concentration during heating period is 1.868 times as much as the mean value during non-heating period, which indicates that the combustion of coal during heating period has a great impact on the rise of PM_{2.5} concentration.

d) Finally, in the Comprehensive analysis of relationship between PM_{2.5} and other indexes of AQI, meteorological factors and heating time, ridge regression equation indicates that SO₂(x₁), NO₂(x₂), PM₁₀(x₃), CO(x₄), the dew point(x₇), visibility(x₁₀) and heating time(x₁₂), compared to other factors, have a significant impact on PM_{2.5}, which have a theoretical guidance for the effective governance and prediction of PM_{2.5}.

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